We Have a DREAM: Distributed Reactive Programming with Consistency Guarantees

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ABSTRACT

The reactive programming paradigm has been proposed to simplify the development of reactive systems. It relies on programming primitives to express dependencies between data items and on runtime/middleware support for automated propagation of changes. Despite this paradigm is receiving increasing attention, defining the precise semantics and the consistency guarantees for reactive programming in distributed environments is an open research problem.

This paper targets such problem by studying the consistency guarantees for the propagation of changes in a distributed reactive system. In particular, it introduces three propagation semantics, namely causal, glitch free, and atomic, providing different trade-offs between costs and guarantees. Furthermore, it describes how these semantics are concretely implemented in a Distributed REActice Middleware (DREAM), which exploits a distributed event-based dispatching system to propagate changes.

We compare the performance of DREAM in a wide range of scenarios. This allows us to study the overhead introduced by the different semantics in terms of network traffic and propagation delay and to assess the efficiency of DREAM in supporting distributed reactive systems.

Categories and Subject Descriptors

C.2.4 [Computer-Communication Networks]: Distributed Systems; D.1.3 [Software]: Concurrent Programming—Distributed Programming

Keywords

Dream, Distributed Reactive Programming, Consistency Guarantees, Glitch-Freedom, Event-Based Middleware

1. INTRODUCTION

Many modern software systems are reactive: they respond to the occurrence of events of interest by performing some computation, which may in turn trigger new events. Examples range from graphical user interfaces, which react to the input of the users, to embedded systems, which react to the signals coming from the hardware, to monitoring and control applications, which react to the changes in the external environment. Designing, implementing, and maintaining reactive software is arguably difficult. Indeed, reactive code is asynchronously triggered by event occurrences. Because of this, it is hard to trace and understand the control flow of the entire system [25].

The reactive programming paradigm [1] was proposed to mitigate these issues and simplify the development of reactive systems. It is based on three key concepts: time-varying values, tracking of dependencies, and automated propagation of changes. To explain the core principles of reactive programming, let us consider the following pseudocode snippets (pseudocode is sans-serif in the rest of the paper) that define a variable a and a variable b that depends on a:

```
1 var a: int = 10
2 var b: int = a + 2
3 println(b) // 12
4 a = 11
5 println(b) // 13
```

In conventional imperative programming (left), any future change to the value of a does not impact the value of b. In reactive programming (right), by defining the second line as a constraint (denoted by :=) rather than a statement, we ensure that b gets constantly updated to reflect the latest value of a. In particular, the runtime environment identifies the dependency between a and b and propagates every change from a to b, forcing the recomputation of the latter.

This solution presents several advantages over the traditional Observer design pattern [20] adopted in event-based architectures to propagate changes. In particular, the programmer does not have to implement the update logic. Instead, she declaratively specifies the dependencies between variables and entirely delegates the update process to the runtime environment. Furthermore, the runtime environment takes care of ensuring the correctness of the propagation. For example, it can avoid the occurrence of glitches, i.e., temporary violations of data flow invariants [6]. This results in more compact and readable code, and reduces the possibility of subtle errors. For example, in 2008 a half of the bugs reported for Adobe’s desktop applications was generated in code for event handling [25].

Despite many reactive applications are intrinsically distributed (e.g., Web applications, monitoring applications, mobile applications) and despite the benefits of reactive pro-
programming in distributed settings have been recognized in the literature \[35, 1, 28\], most existing solutions for reactive programming do not support distribution \[1\]. Furthermore, the problem of defining suitable properties and consistency guarantees for the propagation of changes (e.g., to avoid glitches) has received little or no attention in distributed implementations \[1, 28\].

We argue that a precise definition of such properties and guarantees is an essential requirement for every system that supports the reactive programming paradigm. We also claim that the programmer should be able to choose the level of guarantees she prefers, based on the requirements in terms of semantics as well as computation and communication costs.

This paper focuses on distributed reactive programming (DRP) and specifically addresses the issues described above. First, it introduces an abstract model for DRP systems and defines some consistency guarantees for the propagation of changes. Starting from this analysis, it proposes three propagation semantics, providing different trade-offs between the changes. Next, the paper presents a concrete implementation of these semantics in a Distributed REActive Middleware (DREAM). DREAM is entirely implemented in Java to promote interoperability with existing software (e.g., Android applications) and exploits the REDS distributed event dispatching system \[10\] to propagate changes. Finally, the paper offers an extensive evaluation of the overhead introduced by the three proposed semantics in terms of network traffic and propagation delay.

To summarize, the paper contributes to the research on reactive programming in several ways: (i) to the best of our knowledge, it represents the first attempt to precisely study the consistency guarantees for the propagation of changes in DRP systems; (ii) it proposes three propagation semantics and extensively studies their costs; (iii) it presents the design, implementation, and evaluation of DREAM, a concrete middleware for DRP.

The rest of the paper is organized as follows. Section 2 presents the reactive programming paradigm and motivates the work. Section 3 introduces an abstract model for DRP and studies desirable consistency guarantees. Section 4 and Section 5 discuss the API and the implementation of DREAM. Next, Section 6 assesses the performance of the middleware. Finally, Section 7 surveys related work and Section 8 concludes the paper.

2. BACKGROUND AND MOTIVATION

To describe reactive programming in more details and to motivate the requirements for different levels of guarantees in the propagation of changes, let us consider a financial application system. The system holds a certain amount of stock options and performs forecast analysis on the stock market. The code snippet below sketches up a possible implementation for such system using reactive programming.

```
1 var marketIndex = InputModule.getMarketIndex()
2 var stockOpts = InputModule.getStockOptions()
3 var news = InputModule.getNews()

4 // Forecasts according to different models
5 var f1 := Model1.compute(marketIndex,stockOpts)
6 var f2 := Model2.compute(marketIndex,stockOpts)
7 var f3 := Model3.compute(marketIndex,news)
8
9 var gui := Display.show(f1,f2,f3)
10
11 var financialAlert := ((f1+f2+f3)/3) < MAX
12 if (financialAlert) decrease(stockOpts)
13
14 var financialAlert_n := computeAlert_n(f1,f2,f3)
15
16 if (financialAlert_n) adjust_n(stockOpts)
```

V1. Mobile application. In the first variant (box V1), the forecasts are transmitted to a GUI in a mobile application that displays their current values. As already discussed, a change in marketIndex triggers a recomputation of f1, f2, and f3. Let us assume that the recomputation of f1 terminates first. The change propagates to the gui, which is updated to display the new value of f1. In this scenario, gui is recomputed with the new value of f1 but still the old values of f2 and f3. The user experiences a temporary inconsistency in the values that are displayed (a glitch, as we will explain soon). However, such an inconsistency does not represent a serious issue for this application: as soon as the new values of f2 and f3 are computed, the gui is refreshed and reflects the current value of marketIndex.

V2. Models aggregator. In the second variant of the system (box V2), forecasts f1, f2, and f3 are aggregated in the financialAlert variable. To prevent money loss, an automated procedure starts selling stock options when the financialAlert issues a warning, i.e. when the mean of f1, f2, and f3 drops below a threshold MAX.

Let us consider again a change in the marketIndex. As in the previous example, as soon as f1 is recomputed, the value of financialAlert is invalidated. However, if the expression associated to financialAlert is immediately recomputed with the new value of f1 but the old values of f2 and f3, financialAlert can hold a wrong value.

For example, let us assume that the following set of changes occurs: f1: 110 → 90, f2: 95 → 111, f3: 90 → 103 and MAX=100. If the mean is recomputed with the new value of f1 and the old values of f2, f3, it amounts to (90+95+99)<100 and the alert is triggered. The error is only temporary, because as soon as f2 and f3 are available, the expression bound to financialAlert is recomputed to the correct value. It is clear, however, that in variant V2 such a behavior is potentially catastrophic. In our example,
the application can place a selling order because the value of financialAlert is temporarily wrong.

The arising of temporary spurious values, commonly referred to as glitches is a well known issue in (local) reactive systems, which control the order of updates to avoid them. In our example, waiting for f1, f2, and f3 before re-computing financialAlert would avoid the occurrence of glitches. In a distributed environment, where different variables can be stored at different nodes, enforcing a specific evaluation order introduces some overhead for node synchronization. Such overhead should be paid only in case glitch freedom is a strict requirement.

V3. Multiple aggregators. In the third variant of the system (box V3), the decision making process is split among n components, each one computing a different financialAlert and taking autonomous decisions on how to adjust the stockOpts variable. The actions of the different components are complementary: however, the system provides the expected behavior only under the assumption that all the components see the changes to f1, f2, and f3 in the same order. For example, if different components see different interleaving of marketIndex and news updates, they may disagree on the value of f3 over time and take contradictory measures to adjust the stockOpts variable.

This variant shows that in some cases glitch freedom is not enough to guarantee the correct behavior of the application and exemplifies the need for a system-wide agreement on the order of updates.

In summary, the previous discussion shows that there is no one size fits all solution. Instead, different levels of consistency guarantees are required and developers must be able to select the best trade-off between performance and consistency for their application.

3. A MODEL FOR DRP

This section introduces a model for DRP and the terminology we adopt throughout the paper. In particular, Section 3.1 presents the entities involved in a DRP system and the operations they perform. Next, Section 3.2 formalizes a set of consistency guarantees for DRP.

3.1 System Architecture

Figure 1 shows the high level view of our model for DRP.

**Components.** We consider a distributed system consisting of n components c1, ..., cn, that can exchange messages using communication channels. We model the state of each component ci as a set of variables Vi = {vij : τj1, ..., τjm : τjm}, where vij represents the name of variable j in component ci and τj its type. We say that a variable vij is defined in the scope of component ci if τij ∈ Vi. Each component can directly access (read and write) only the value of variables defined in its scope.

**Dependencies.** The edges between components represent the dependencies that lead to recomputation of a variable. In particular, we say that a variable vij is dependent on a variable vik if vik has a direct dependency on variable vij.

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3.2 Consistency Guarantees

**Observable variables.** Observable variables are those that can be used to build reactive expressions. In the stock market scenario in Section 2, marketIndex, stockOpts, and news are observable variables, used in the definition of f1, f2, and f3. Our model supports local observable variables, that are only visible in the scope of component ci, and global observable variables can be used in every component. By default, observable variables are global. A fundamental feature to support compositionality is that reactive variables can be (locally or globally) observable as well. This way, reactive variables can be composed into reactive expressions to create new reactive variables. For example, in the stock market scenario of Section 2, the reactive variables f1, f2, and f3 are used to define another reactive variable gui.

**Dependency Graph.** We call dependency graph a directed graph D = (V, E), where V is the set of all the observable and reactive variables in the system and E is the set of all the edges eij that connect a variable vi to a variable vj if and only if vj is a reactive variable defined through an expression eij that includes vi. We say that a variable vn depends on a variable vj if there is a path from vj to vn. As an example, the stock market scenario in Section 2 produces the dependency graph shown in Figure 2. The gui variable depends on both marketIndex, stockOpts, and news.

Reactive programming needs to be supported by the runtime environment, which is responsible for automatically and recursively propagating the changes from a variable vi to all the variables that depend on vi.

**Events.** We represent the occurrence and the propagation of changes in a DRP system using three events that model the possible operations on the variables in the system:

- a write event w_x(v) occurs when a component writes the value x on an variable v;
- a read event r_x(v) occurs when a component reads the value x from a variable v;
- an update event u(S, w_x(v)), S = {w_x1(v1) ... w_xn(vn)} occurs when some changes applied to variables v1 ... vn
(for simplicity, known in advance) are propagated, triggering a change (write of a new value \(x\)) in the depending reactive variable \(v\).

The read and write events represent the way components access local variables. We assume that these operations are atomic. Update events model the propagation of changes through the communication channel. Next, we show how to specify some consistency guarantees for DRP as ordering of write and update events.

### 3.2 Consistency Guarantees

The update of reactive variables takes place orthogonally with respect to the execution flow of the program in each component. Accordingly, it is critical for the programmer to understand how the update process takes place, and in particular which properties and guarantees it provides, e.g., with respect to the order in which updates are propagated. We collectively refer to them as consistency guarantees.

Intuitively, there is a trade-off between the level of guarantees offered and the complexity of the update algorithm. Ideally, a change in an observable variable should be propagated atomically and instantaneously through the dependency graph to all the reactive variables that depend on it. This section studies in details some consistency guarantees for DRP systems.

**Exactly once delivery.** A system provides exactly once delivery if a change in the value of a variable \(v\) is propagated once and only once to all variables depending on \(v\). More formally, if \(w_2(v)\) occurs, then \(u(S_1, w_2(v_1))\), \(w_2(v) \in S_1\) occurs once and only once \(\forall v_0\) such that \(v_1\) depends on \(v\).

This property ensures that, in absence of failures, the communication channel does not loose or duplicate any message used for the propagation of changes.

**FIFO ordering.** A system provides FIFO ordering if the changes to the value of a variable \(v\) in component \(c\) are propagated in the order in which they occur in \(c\). More formally, \(\forall u_1, v_1\) such that \(v_1\) depends on \(v\), if \(w_2(v)\) occurs before \(w_3(v_1)\), then \(u(S_1), w_2(v_1) \in S_1\) occurs before \(u(S_2), w_3(v_1) \in S_2\).

**Causal ordering.** A system provides causal ordering guarantee if the events that are potentially causally related are seen by every component of the system in the same order. More formally, with reference to [22], we define a happened before \((\rightarrow)\) partial order relation between the events in a DRP system as follows:

- if two events \(e_1, e_2\) occur in the same process, then \(e_1 \rightarrow e_2\) if and only if \(e_1\) occurs before \(e_2\);
- if \(e_1 = w_2(v)\) and \(e_2 = u(S, w_3(v))\), \(w_2(v) \in S_1\), then \(e_1 \rightarrow e_2\) (a write \(w\) happens before every update \(u\) depending on \(w\));
- if \(e_1 \rightarrow e_2\) and \(e_2 \rightarrow e_3\), then \(e_1 \rightarrow e_3\) (the happened before relation is transitive).

We say that a system provides causal consistency guarantee if and only if, for all events \(e_1, e_2\) such that \(e_1 \rightarrow e_2\), all the components of the DRP system see \(e_1\) before \(e_2\). Notice that the happened before is a partial order relation: events that are not causally related can be seen in any order by different components. Because of this, the causal ordering guarantee does not imply that all components see all events in the same order.

**Glitch freedom.** Consider a reactive variable \(v\) that depends on the set of variables \(V_d\). Let us call \(V_d \subseteq V_q\) the set of variables in \(V_q\) that depend, directly or indirectly, from a variable \(v_i\). Each change in variable \(v_i\) reflects on variable \(v\) since it impacts on the variables in \(V_d\). We call an update of \(v\) \(u(S, w_2(v))\) a partial update if it is triggered by a change in \(v\) and \(S \subseteq V_d\) (i.e., \(S\) does not propagate all the changes occurred in the set \(V_d\)). A system provides glitch freedom if it never introduces partial updates.

To better explain this concept, let us refer again to the stock market monitoring scenario shown in Section 2. When the value of marketIndex changes, it influences the forecasts \(f_1, f_2\), and \(f_3\). With reference to the financialAlert variable, a glitch occurs if the variable gets recomputed using only some of the new forecasts (partial update). No glitch occurs if financialAlert is recomputed only when all the new values for \(f_1, f_2\), and \(f_3\) are available.

**Atomic consistency.** A system provides atomic consistency guarantee if the following conditions hold: (i) the system provides FIFO ordering guarantee; (ii) each write event \(w_2(v)\) on a variable \(v\) is atomically propagated to all the variables that depend (directly or indirectly) on \(v\), i.e., all the update events \(u(S_i, w_3(v))\) triggered (directly or indirectly) by \(w_2(v)\) are executed in a single atomic operation.

Intuitively, the atomic consistency guarantee ensures total order of events (it is more strict than the causal order guarantee). At the same time, it also ensures atomicity of propagation: no operation can occur while a propagation is taking place. Finally, since propagations occur atomically, it also ensures glitch freedom.

### 4. DREAM: API

This section describes the API of DREAM. To promote interoperability with existing codebases, DREAM is entirely written in Java. In particular, variables are represented by Java objects. The remainder of this section shows how to define, instantiate, and use observable and reactive objects.

#### 4.1 Observable Objects

In DREAM, observable objects are generic Java objects that inherit from the Observable abstract class. As for every Java object, the internal state of an observable object can be accessed (read or modified) through method invocation. We call observable method each method of an observable object that returns a non-void result.

Let us consider an observable object \(\text{obj}\) with an observable method \(\text{obm}\) and a generic method \(m\). We say that \(m\) impacts on \(\text{obm}\) if a call to \(m\) on \(\text{obj}\) may potentially change the return value of \(\text{obm}\).

As discussed in the following, an observable method \(\text{obm}\) can be used to define a reactive object. For this reason, the runtime environment needs to capture every call to a method that impacts on the value of \(\text{obm}\) and propagate the change to any depending reactive objects\(^1\).

An automated detection of the impacts on relation among methods is undecidable in the general case [37]. DREAM solves this problem by asking the programmer to make this decision.

\(^1\)We assume that the state of an observable object can be altered only through method invocation. This is a best engineering practice in object oriented programming.
relation explicit through an ad-hoc Java annotation. An approximation using static analysis is left for future work.

Listing 1 shows the definition of a simple Observable class: ObservableInteger. As Listing 1 shows, defining a new type of observable objects in DREAM requires two actions. (i) inherit from the Observable abstract class. (ii) annotate each method with its set of observable methods it impacts on, by using the @ImpactsOn annotation. For example, in Listing 1, set impacts on observable method get since a call to set modifies the value of variable val that is read by get. DREAM provides built-in observable types for integers and floating point numbers, strings, and different kinds of collections. Users can create new classes of observable objects using the procedure above.

The instantiation of observable objects is shown in Listing 2, Lines 2-5. The code snippet is commented in details in the rest, after introducing DREAM support for naming and discovery.

### 4.2 Reactive Objects

In DREAM, a reactive object is created from a reactive expression using the ReactiveFactory class. A reactive expression can combine constant values and return values of observable methods. For example, the reactive object generated in Listing 2, Line 9, contains an integer value defined from the observable method get of object obInt and the constant value 2. The reactive object generated in Line 11 contains a string value defined from two observable methods get from objects obStr1 and obStr2. The value of a reactive object cannot be directly modified, but only retrieved by invoking a get method (Line 14).

When defining a reactive object r in DREAM, the programmer can specify two initialization semantics. The blocking semantics blocks every read access to r until the current values of all the observable methods r depends on have been retrieved and the value of r has been successfully computed. The non-blocking semantics enables the programmer to specify an initial value that the variable holds until its expression can be computed.

Similar to observable objects, DREAM provides several built-in types of reactive objects. Programmers can use them to define the state of more complex objects. Additionally, they can define their own types of reactive objects and the expressions to combine them.

### 4.3 Naming and Discovery

In DREAM, we assume that a unique name identifies each component of the distributed system. Similarly, a (locally) unique name identifies each observable object inside a component. The programmer can reference an observable method get of an object obj inside a component c using the notation c.obj.get(). The name of the component can be omitted when referencing a local object.

The name of an observable object and, optionally, its visibility (local or global) are assigned at instantiation time. For example, consider Listing 2. The statements in Lines 2-6 are executed in component c1. Line 2 defines an ObservableInteger object announced as obInt1, an initial value of 1, and local visibility. Line 4 defines an ObservableString object announced as obStr1, initial value a, and global visibility. Reactive objects can also be defined as observable by simply specifying a name for them. For example, Line 19 in Listing 2 (executed in component c3) defines a ReactiveInteger object that contains the length of string c1.obString1 and makes it an observable object by associating a unique name to it (obString1Len). Since no additional parameters are specified, the object has default global visibility.

To discover the observable objects available in the system, DREAM offers a flexible discovery service. It allows a component to retrieve the full name of observable objects searching by type, component, local name, or a combination of these fields.

### 5. DREAM: IMPLEMENTATION

This section describes the implementation of DREAM in details, showing the protocols for automated propagation of changes in a distributed environment, and discussing the consistency guarantees they offer. Figure 3 shows the architecture of the middleware, which implements the abstract model presented in Figure 1.

DREAM consists of two parts: a client library, adopted by each component of the distributed system (denoted as c in Figure 3) and a distributed event-based communication infrastructure, consisting of one or more brokers (black circles in Figure 3) connected to form an acyclic undirected overlay network. The broker infrastructure implements the communication channel between components. An optional registry (R in Figure 3) acts as a persistent storage.

#### 5.1 Publish-Subscribe Communication

In DREAM, the propagation of changes from observable to reactive objects is implemented using a publish-subscribe
that 

CommunicationManager 

advertise(c,obj,obm) - 

primitives: 

communication paradigm [15], based on the following three 

new value to the 

CommunicationManager 

putes the value of each of these methods and notifies the 

CommunicationManager 

informs the 

able object 

serves two purposes. (1) Advertise new observable ob-

additional effort for the programmer. The interaction 

DREAM 

automatically weaves a 

Instantiating observable and reactive objects. 

when the programmer instantiates a new reactive object 

the core functionalities of the DREAM client library. It man-

We refer to the content of these primitives as advertise-

method, we say the subscription matches the advertise-

Similarly, if a subscription and a notification refer to the same 

method, we say that the notification matches the subscrip-

5.2 Clients 

The CommunicationManager component implements 

the local communication among objects inside the same 

component and serves as a proxy for global communication 

involving multiple components. 

Instantiating observable and reactive objects. When 

the program defines a new type of observable object, 

DREAM automatically weaves a Watcher advice, using 

aspect-oriented technology [21]. The Watcher advice in-

CommunicationManager without any 

additional effort for the programmer. The interaction 

serves two purposes. (1) Advertise new observable ob-

jects as soon as they are created. When a new observ-

able object obj is instantiated, the Watcher notifies the 

CommunicationManager that obj has been created and 

informs the CommunicationManager of each observable 

method in obj. (2) Detect changes of the return value of the 

observable methods in obj. For each method m of obj, the 

Watcher uses Java reflection to identify all the observable 

methods influenced by m, as specified by the ImpactsOn 

annotation. When m is called on obj, the Watcher recom-

putes the value of each of these methods and notifies the 

new value to the CommunicationManager. 

When the programmer instantiates a new reactive object 

with expression exp via the ReactiveFactory, DREAM 

automatically forwards to the CommunicationManager a 

subscription for each observable method in exp. 

When a component c is launched, the 

CommunicationManager of c connects to a single 

broker of the communication infrastructure. It propagates 

through the broker all the advertisements generated by 

(global) observable objects defined in c and receives sub-

scriptions for them. In addition, it stores subscriptions of 

local reactive objects. 

Notifications. Upon receiving a notification n (either from 

the remote broker or from a local observable object), the 

CommunicationManager dispatches it to all interested ob-

jects, i.e., to all the reactive objects providing a subscription 

that n matches. If n is a local notification matching at least 

one remote subscription, the CommunicationManager also 

delivers n to the remote broker. 

In DREAM, each component is responsible for concretely 

computing the expression expr for each reactive object obj 

defined in its scope. In particular, a recomputation is trig-

gered upon receiving a new notification of change from the 

CommunicationManager. In the case of causal consist-

tency, each change event can be processed immediately. In 

contrast, glitch freedom may require that the evaluation of 

a change is postponed until other notifications are received. 

As we describe soon, the broker network is responsible for 

detecting dependencies among events and notify them to the 

component. The CommunicationManager employs this 

information to temporarily queue notifications until they can 

be processed without introducing glitches. 

The CommunicationManager implements the commu-

nication within a single component using local method in-

vocation. Thus, propagating the change of an observable 

method to a reactive object in the same component does 

not involve any overhead due to remote communication.

5.3 Brokers 

The communication between brokers is implemented using 

the subscription forwarding protocol [8] on top of the REDS 

event dispatching system [10]. This protocol relies on the 

assumption that the brokers are connected into an acyclic 

topology and works in three steps: (i) Advertisements are 

propagated to all the brokers of the network. (ii) Subscrip-


tions get propagated only towards components that pro-

vided matching advertisements. (iii) Similarly, notifications 

are propagated only towards components that provided a 

matching subscription. 

The forwarding algorithm implemented by brokers is 

shown in Listing 3 (simplified for the presentation). Each 

broker maintains a list of all its neighbors, i.e., all the nodes 

(both brokers and components) directly connected to it. 

Also, it stores the list of advertisements received from each 

neighbor (advTable in Listing 3) and the list of subscrip-


tions received from each neighbor (subTable in Listing 3). 

Upon receiving an advertisement adv (function processAdv in 

Listing 3), the broker first updates the advTable structure and 

then forwards adv to all its neighbors, except the sender. 

Similarly, upon receiving a subscription sub (function processSub in 

Listing 3), the broker first updates the subTable structure, then 

looks for the neighbor with an advertisement that matches sub 

and forwards the subscription to it. Finally, upon receiving a 

notification n (function processNotify in Listing 3), the
4.4 Implementing Consistency Guarantees

DREAM offers three propagation semantics with an increasing level of consistency guarantees. (i) Causal semantics provides exact once delivery with causal ordering. (ii) Glitch free semantics, adds glitch freedom. (iii) Atomic semantics, implements atomic consistency.

Causal Semantics. In DREAM, both the component-to-broker communication and the broker-to-broker communication are implemented using point-to-point TCP connections, which provide exactly once delivery guarantee and FIFO order. To ensure that FIFO order is preserved between any given pair of components, processing inside each intermediate broker must preserve message ordering. Currently, DREAM ensures this property by processing messages sequentially, in a single thread. Alternative implementations that feature parallel processing should take care of reordering messages before delivery.

Finally, as proved in [19], an acyclic topology that preserves end-to-end FIFO ordering is sufficient to ensure that messages are delivered in causal order.

As mentioned in Section 5.2, in DREAM, each reactive object obj is responsible for recomputing the value of its own expression expr. In the case of causal consistency, obj immediately starts a recomputation upon receiving a notification from an observable object defined in expr. No further constraints are required to ensure causal consistency.

Glitch Free Semantics. Existing solutions for reactive programming provide glitch freedom on single machine implementations by propagating changes in the dependency graph in topological order (breadth first). This ensures that an expression is always evaluated after all its dependents [6, 30, 25]. To achieve the same result in a distributed environment, we modified the algorithm for the propagation of updates described in Listing 3 as follows.

First, when a new reactive object is created, its defining expression is propagated to all the brokers in the communication infrastructure. This way, each broker gains complete knowledge of the graph of dependencies among objects and can identify possible sources of glitches. With reference to the definition provided in Section 3.2, a glitch occurs when the value of an observable method changes and the value of a depending reactive object is updated before seeing all the effects of the original change.

Let us consider again our stock market scenario. For ease of explanation, the dependency graph for the variant V2 of the system is shown in Figure 4. We assume that each variable is stored on a different component.

In this example, a glitch occurs if a change in marketIndex affects the values of f1, f2, and f3, but financialAlert gets updated upon receiving only some notifications of change (e.g., only from f1). We refer to such a notification as a partial update, since it does not contain all consequences of the original change in marketIndex.

To prevent glitches, DREAM implements a queuing mechanism, such that partial notifications are temporarily stored at the components until all the consequences of a change become available. Specifically, before delivering a notification n to a component c, a broker computes the set of additional notifications that c needs to receive before processing n and attaches this information to the message containing n. With reference to our example in Figure 4, when a broker delivers a notification about a change in f1 to financialAlert, it specifies that n can be processed only if two notifications about f2 and f3 have been received.

Notice that, when processing n, a broker cannot determine the set of notifications a component should wait for by looking only at the content of n. In our example, a change in f3 could be triggered either by a change in marketIndex or by a change in news. In the first case, the expression defining financialAlert can be recomputed immediately upon the reception of n. In the second case, the expression

5.4 Implementing Consistency Guarantees

DREAM offers three propagation semantics with an increasing level of consistency guarantees. (i) Causal semantics provides exactly once delivery with causal ordering. (ii) Glitch free semantics, adds glitch freedom. (iii) Atomic semantics, implements atomic consistency.

Causal Semantics. In DREAM, both the component-to-broker communication and the broker-to-broker communication are implemented using point-to-point TCP connections, which provide exactly once delivery guarantee and FIFO order. To ensure that FIFO order is preserved between any given pair of components, processing inside each intermediate broker must preserve message ordering. Currently, DREAM ensures this property by processing messages sequentially, in a single thread. Alternative implementations that feature parallel processing should take care of reordering messages before delivery.

```
1 Map<Node, List<Advertisement>> advTable;
2 Map<Node, List<Subscription>> subTable;

4 void processAdv(Advertisement adv, Node sender) {
5    advTable.add(adv, sender);
6    sendToAllNodeExcept(sender, adv);
7 }
8 
9 void processSub(Subscription sub, Node sender) {
10    subTable.add(sub, sender);
11    for (Node node : advTable.keySet()) {
12        List<Advertisement> advs = advTable.get(node);
13        if (!node.equals(sender) && matches(sub, advs)) {
14            sendToNode(node, sub);
15            break;
16        }
17    }
18 }
19 
20 void processNotif(Notification n, Node sender) {
21    for (Node node : advTable.keySet()) {
22        List<Subscription> subs = subTable.get(b);
23        if (!node.equals(sender) && matches(n, subs)) {
24            sendToNeighbor(node, n);
25        }
26    }
27 }
```

Listing 3: Forwarding algorithm implemented in brokers

Brokers forwards n to all the neighbors with at least one subscription matched by n.

Discovery and Initialization. As discussed above, advertisements of globally visible observable objects are delivered to all brokers of the network. This allows DREAM to replicate the discovery service at each broker. Specifically, when a component c connected to a broker B issues a lookup request (to retrieve observable objects by name, type, or component), B can process the request locally, based on the information contained in its list of advertisements.

Concerning initialization, when a new reactive object is defined with an expression exp, the DREAM client library forwards a subscription for each observable method in exp. This subscription triggers a retransmission of all the latest observable methods, enabling the new reactive object to be initialized.

Finally, DREAM also allows observable objects to be persisted: each notification of change is stored in a special broker (the Registry R in Figure 3). Thanks to this solution, if the component defining an observable object obs disconnects from the system, the latest value of all the observable methods defined for obs can still be retrieved from R.

Figure 4: The dependency graph for the stock market system (Variant V2).
cannot be recomputed until the new values of $f2$ and $f3$ (also influenced by a change in marketIndex) are propagated. Because of this, a broker must be aware of the history of changes that caused the notification under processing. In case of glitch free semantics, DREAM attaches this information to each event notification. In our example, a notification about a change in $f3$ caused by marketIndex will be labeled with marketIndex. Similarly, a notification about a change in $f3$ caused by news will be labeled with news.

Since the dependencies are always computed in the broker network, the glitch free protocol introduces a significant difference with respect to the causal protocol: it always requires notifications to be forwarded through the broker network. Conversely, in the causal consistency protocol, each component (and in particular the ConnectionManager within each component) could dispatch notifications to local subscribers without contacting the broker network.

Finally, it is easy to see that the protocol for glitch freedom preserves causal ordering since the properties of the communication infrastructure are not changed. The broker-to-broker network is acyclic and guarantees exactly once delivery. FIFO order is preserved since notifications are always delivered inside the broker network. Crucially, the queuing mechanism implemented at the components does not change message order. A notification waits in the queue until all the notifications related to the same reactive expression arrive, which may result in a delay in the expression evaluation but not in a change in the message order.

**Atomic Semantics.** The atomic semantics adds total order of changes on top of the glitch free semantics. DREAM ensures total order by implementing a locking mechanism based on a special centralized component in the communication infrastructure: the Ticket Granting Server (TGS). Upon receiving a new change notification $n$ from an observable method $obm$, a broker $B$ contacts the TGS to obtain the right of propagating the change to all the reactive objects that (directly or indirectly) depend on $obm$. The protocol works as follows: (i) $B$ sends $n$ to the TGS. (ii) The TGS computes all the leaves in the dependency graph that $n$ should reach. (iii) The TGS stores the notifications in a FIFO queue and delivers them to the broker network one at a time. (iv) While processing a notification, when a broker $B$ sends an update for a leaf in the dependency graph, it notifies the TGS. Upon receiving an acknowledgement of delivery to all the leaves in the dependency graph, the TGS considers the propagation of a change completed, and starts the propagation of the next change in the queue.

Since the protocol used in the communication infrastructure is identical to the one described for glitch freedom, all guarantees introduced in the previous sections are preserved. The use of a locking mechanism adds the guarantee that only one component at a time can execute an update.

6. EVALUATION

Our evaluation is twofold. First, we perform a comparative assessment of the cost of ensuring different consistency levels and analyze the factors that influence such a cost. Second, we investigate the absolute performance of our current implementation – including communication overhead and evaluation of reactive expressions – to show that DREAM is usable in practice.

For the first goal, we created an emulated network using the Protopeer network emulator [16], on top of which we run multiple DREAM brokers offering the DRP service to several components. This allowed us to easily control a number of network parameters. For the second goal, we tested the processing and communication overhead of DREAM on a real machine.

### 6.1 Analysis of the Protocols for DRP

In this first set of experiments, we compare the costs of our DRP protocols while providing different levels of consistency guarantees. We focus on two metrics: network traffic and propagation delay. To compute network traffic, we consider both component-to-broker communication and broker-broker communication and we measure the average traffic flowing in the entire network every second. To compute propagation delay we compute the average difference between the time an event is produced, i.e., when the value of an observable object $obs$ changes, and the time an event is processed, i.e., the change is used to update the value of a reactive object that depends (directly or indirectly) on $obs$.

**Experiment Setup.** Several parameters can impact on the performance of our protocols. To isolate their effect, we defined a default scenario, whose values are listed in Table 2. Next, we performed several experiments, changing a single parameter in each one.

Our default scenario consists of 10 brokers connected in a randomly-generated scale-free overlay network and serving 50 components. We assume that 50% of the brokers are pure forwarders, i.e., do not have any directly connected component. Components are uniformly distributed among the remaining brokers. The latency of network links is uniformly distributed between 1 ms and 5 ms. We assume that the time required to process a packet is negligible with respect to the link latency.

We consider 10 separate dependency graphs, each of them including an observable object (the original source of changes) and 4 reactive objects that depend directly or indirectly from it. Each reactive object is defined by a randomly generated expression including 2 operands (on average). Each observable object changes its value every second (on average). To simulate different application loads, we introduce a locality parameter: given a reactive object $r$ depending on an observable object $obs$, the locality parameter defines the probability that $r$ and $obs$ are defined in the same component. With locality $l$, all objects of the graph are deployed on a single component. Conversely, with locality 0, objects are randomly distributed over all available components.

Our experiments consist of two phases. In the first phase

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Number of brokers</td>
<td>10</td>
</tr>
<tr>
<td>Number of components</td>
<td>50</td>
</tr>
<tr>
<td>Topology of broker network</td>
<td>Scale-free</td>
</tr>
<tr>
<td>Percentage of pure forwarders</td>
<td>50%</td>
</tr>
<tr>
<td>Distribution of components</td>
<td>Uniform</td>
</tr>
<tr>
<td>Link latency</td>
<td>1 ms–5 ms</td>
</tr>
<tr>
<td>Number of reactive graphs</td>
<td>10</td>
</tr>
<tr>
<td>Size of dependency graphs</td>
<td>5</td>
</tr>
<tr>
<td>Size of reactive expressions</td>
<td>2</td>
</tr>
<tr>
<td>Degree of locality in expressions</td>
<td>0.8</td>
</tr>
<tr>
<td>Frequency of change for observable objects</td>
<td>1 change/s</td>
</tr>
</tbody>
</table>

Table 1: Parameters used in the default scenario.

---

3 Several algorithms have been presented in the literature for efficient event dispatching [26, 27, 34]. Further, Section 6.2 validates the assumption using the current DREAM implementation.
Advantages of Distribution. Our first experiment investigates the advantage of using a network of brokers for the DRP service. We compare a centralized solution with the distributed solution in our default scenario. More in particular, the two solutions consider the same (physical) network topology, but deploy a different number of brokers (1 in the centralized scenario, 10 in the distributed scenario).

Table 2 shows the results we measured: the level of consistency guarantees significantly influences the performance of DREAM in both scenarios. Let us first consider the average change propagation delay. The differences we measured in the default (distributed) scenario (Table 2, Column 2) can be explained as follows. When providing causal consistency, each component processes local changes without contacting the broker network. Since our default scenario exhibits a high degree of locality in expressions, most changes can be processed within components. In contrast, the protocol for glitch freedom requires each and every event to be processed by at least one broker. Atomic consistency requires additional communication to acquire the lock from the TGS.

If we consider the centralized scenario (Table 2, Column 1), we observe that, in the case of causal consistency, the delay is almost identical to the one measured in the distributed scenario. Also in this case, most of the events can be processed locally at components. In contrast, the protocols for glitch freedom and atomicity forward all the events though the centralized broker. While in our default scenario the filtering and forwarding of events was performed incrementally at each broker, as close as possible to the event source, in a centralized environment all events need to reach the single broker to be processed and forwarded, which causes a significant increase in the average delay.

The considerations above apply for network traffic as well (Table 2, Columns 3-4). The causal consistency protocol needs to forward less notifications, the protocol for glitch freedom and atomic consistency are comparable, but the latter produces more traffic because it includes the communication with the TGS. We can conclude that the idea of adopting a distributed broker network for the propagation of changes offers significant benefits in terms of network traffic and propagation delay.

Table 2: Centralized vs. distributed broker networks.

<table>
<thead>
<tr>
<th></th>
<th>Causal</th>
<th>Glitch free</th>
<th>Atomic</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Centr. Delay (ms)</strong></td>
<td>7.77</td>
<td>4.76</td>
<td>60.3</td>
</tr>
<tr>
<td><strong>Distr. Delay (ms)</strong></td>
<td>17.18</td>
<td>205.4</td>
<td>130.9</td>
</tr>
<tr>
<td><strong>Centr. Traffic (KB/s)</strong></td>
<td>29.53</td>
<td>68.3</td>
<td>265.5</td>
</tr>
<tr>
<td><strong>Distr. Traffic (KB/s)</strong></td>
<td>17.18</td>
<td>29.53</td>
<td>265.5</td>
</tr>
</tbody>
</table>

Locality of Expressions. The previous experiments show the capability of the causal consistency protocol to exploit locality. To further investigate this aspect, we tested the performance of DREAM when changing the degree of locality (Figure 5). All protocols reduce the average propagation delay as the degree of locality increases (Figure 5a): indeed, as the locality increases, the number of brokers used to forward an event decreases. As expected, the causal consistency protocol benefits more than the others from the increased degree of locality.

The results concerning network traffic (Figure 5b) are particularly interesting. The glitch free and the atomic protocols generate similar amounts of traffic – the latter being slightly more expensive because of the communication with the TGS. Noticeably, the traffic generated by the protocol for causal consistency drops much faster than the others as the degree of locality increases.

The presence of glitches explains the worse performance of the causal consistency protocol with a very low degree of locality (<0.2). When a glitch occurs, an intermediate node in a dependency graph is reevaluated (and thus triggers new change notifications) every time it receives a partial update. Conversely, protocols for glitch freedom that accumulate partial changes before triggering a new reevaluation are more efficient in this case.

Size of Reactive Graphs. Figure 6 shows the performance of DREAM when changing the size of the dependency graphs, i.e., the number of (observable and reactive) objects included in each graph. As expected, the propagation delay increases with the size of the graph (Figure 6a) because, on average, more steps are required to propagate the changes to all the interested reactive objects. The overall network traffic also increases with the size of the graph. Interestingly, the size of the graph has a more significant impact for the causal consistency protocol, since it produces more glitches and consequently more (redundant) expression evaluations.

Size of Reactive Expressions. Figure 7 shows the impact of the size of reactive expressions (i.e., the number of observable objects appearing in each expression) on the performance of DREAM. Increasing the number of objects in each expression (with a fixed degree of locality) increases
the number of notifications from remote objects that are required to evaluate the expression. For this reason, the delay increases for all protocols (Figure 7a). However, the delay increases faster with protocols for glitch freedom and atomicity, which need to receive all the notifications before processing them. Conversely, the causal protocol always processes (local) notifications immediately, without waiting for remote objects. The same considerations explain why increasing the number of objects in each expression also increases the overall network traffic (Figure 7b). In this case, the causal protocol is more affected: indeed, a higher number of dependencies between objects reflects in a higher number of potential glitches, and consequently a higher number of partial updates (not generated by the glitch free and the atomic protocols). However, the number of potential glitches in the graph stabilizes after 3 objects, and the traffic does not increase further.

6.2 Efficiency of DREAM

In the previous section, we evaluated DREAM with a network emulator to easily control a number of parameters. Since the network emulator did not consider the processing times (both at the clients and at the brokers), all results we collected are valid under the assumption that the processing time is negligible with respect to network latency (i.e., processing does not the bottleneck). We now validate this assumption, assessing the performance of DREAM.

To isolate the costs of event processing, we consider a local scenario, where a component C and a broker B are deployed as two separate Java processes on the same machine. The component defines an observable object obs of type double and a reactive object r that depends on obs. In the test, we increased the complexity of the expression that defines r, introducing an increasing number of (arithmetic) operators applied to obs. Figure 8 shows the delay introduced by the DREAM middleware to propagate changes from obs and to recompute the expression that defines r.

In the case of causal consistency, the processing is local to the component: each change to obs generates an event that is passed to r using local method invocation and triggers the recomputation of the reactive expression. This experiment evaluates the cost of intercepting a method call, propagate the change, and reevaluate the expression using the code generated by ANTLR. We measure a delay that is lower than 0.15 ms with up to 10 operators and lower than 1 ms even in the extreme case of 1000 operators.

In the case of glitch free consistency, the propagation involves the broker B. In this case, the time we measure includes two communication steps (from C to B and back), which require serialization and deserialization of every event and processing at B. This process introduces a modest additional delay of about 1 ms with respect to causal consistency. Finally, the atomic consistency protocol introduces an additional communication step to contact the TGS. Based on these results, we can confirm the assumption of the previous section.

6.3 Discussion and Outlook

To the best of our knowledge, this work is the first attempt to investigate different consistency guarantees for DRP. Our evaluation demonstrates the validity of the major design choices of DREAM and suggests guidelines for future research.

First, our analysis shows the benefits of a distributed infrastructure for the propagation of changes, both in terms of network traffic and propagation delay. As expected, this advantage increases in scenarios where data accesses exhibit forms of locality. Since there is no single point of failure, a decentralized architecture provides an optimal starting point to explore fault-tolerant solutions. Currently, DREAM only supports caching though a globally accessible registry in case a value cannot be retrieved from a node. Future research should focus on how to keep the reactive network operational even when certain nodes are temporarily unresponsive.

Second, we observe that our protocol for causal consistency is usually more efficient than the others, since it enables components to autonomously dispatch local changes. On the other hand, it can potentially produce more traffic and demand for a higher number of expression evaluations due to the presence of glitches. This circumstance demands for an infrastructure that (i) supports different consistency protocols inside (different parts of) the same reactive system and (ii) can switch among them to optimize performance.

It is worth noticing that the glitch free protocol could be optimized to process local changes in a component, without contacting external brokers – in case this cannot introduce glitches. This would require, however, a complete knowledge of the dependency graphs at each component. For this reason, we decided not to implement this solution in DREAM.

Finally, providing atomic consistency does not significantly impact on the overhead of DREAM when the rate of changes remains low. However, it prevents from running multiple propagations concurrently: because of this, in presence of high rate of changes, notifications would be queued at the TGS, with a negative impact on propagation delay.

7. RELATED WORK

Given the cross-field nature of our research, we organize related work in (i) reactive programming and (ii) event-based systems.

Reactive programming. Reactive programming refers to language abstractions and techniques to model and support time changing values. It was originally proposed in the context of strictly functional languages. Specifically, functional reactive programming (FRP) was first introduced in Haskell to support interactive animations [11].

Recently, reactive programming has gained increasing attention, and several implementations have been developed for various programming languages. We report only the

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\[ \text{Figure 8: Efficiency of DREAM.} \]
most prominent examples; the interested reader can find a recent and detailed survey on reactive programming in [1].

In the context of functional languages, Fran [11, 12] and Yampa [18] extend Haskell with two first class concepts to express time-varying values, behaviors for modeling continuous values and events for modeling discrete changes. Similar to DREAM reactive objects, behaviors can be combined and various Haskell operators were adapted to work with behaviors. Analogous extensions have been proposed for Scheme (see FrTime [5]) and Scala (Scala.React [25], REScala [36]). In contrast to DREAM, these solutions target only the local setting. Interestingly, in [12] the authors propose hybrid push/pull-based propagation of changes: the former reevaluates a reactive expression as soon as a change is detected, making the new updated value always available; the latter postpones the evaluation until it is strictly required, potentially reducing the computational effort. DREAM implements a pure push-based propagation model: we plan to investigate the feasibility and benefits of pull-based propagation in future work.

Similar to DREAM, Frappe [7] is a reactive programming library for Java. It extends the JavaBeans component model [4] introducing event sources (similar to DREAM observable objects) and behaviors (similar to DREAM reactive objects). Despite these similarities, Frappe does offer distributed deployment.

In the context of Web programming, Flapjax [30] has been proposed as a reactive programming library for JavaScript. The design of Flapjax is mostly based on FrTime. Flapjax supports distribution to enable client/server communication, but, as acknowledged by the authors, glitches are not avoided in distributed reactive applications.

AmbientTalk/R [23] is a reactive extension to AmbientTalk, an actor-based language for mobile applications. Similarly to Flapjax, AmbientTalk/R supports distributed reactive programming but does not ensure consistency guarantees or glitch avoidance.

The need for DRP with consistency guarantees has been widely recognized in literature [28, 1, 35]. Similarly, the integration of reactive and object-oriented programming have been discussed in [37]. In future work, we plan to explore this integration in more detail, focusing on solutions for automated tracking of dependencies, better support for inheritance, and efficient strategies for recomputation of values.

Reactive programming has been influenced by other paradigms based on dataflow and synchronous propagation of change. Synchronous programming [3] is one of the earliest paradigms proposed for the development of reactive systems. It is based on the synchrony assumption, i.e., it assumes reactions to be instantaneous and atomic. This assumption simplifies the program, which can be compiled into finite-state automata. Dataflow programming [39] represents programs as directed graphs, where nodes represent computations and arcs are dependencies between them.

Event-based systems. Event-based systems [31] define a model for dealing with reactive applications that is complementary to the one described in this paper. In reactive programming, events (notifications of changes) are implicit and reactions (recomputation of reactive variables) are declaratively specified. Conversely, in event-based systems events are explicitly notified using call-back functions and the programmer can imperatively specify custom reactions.

DREAM currently relies on a publish-subscribe infrastructure [15] for the propagation of events. In addition to event forwarding, Complex Event Processing (CEP) systems [9, 24, 13] provide operators for event composition. For example, they enable to detect (temporal) patterns or apply functions over all the events received in a given time window. We plan to exploit these features to extend the expressiveness of DREAM. The interested reader can refer to our paper [28], where we compare reactive programming and CEP systems and provide a roadmap for integrating them.

Concerning consistency guarantees, [40] discusses ordering guarantees for publish-subscribe systems. Similarly, [2] presents an analysis of consistency in the domain of CEP.

In the context of event-based systems, it is worth mentioning that several libraries and language extensions have been proposed to support events and event composition as first class language constructs. The most notable examples are EventJava [14], Ptolemy [33], ESCala [17] and JEScala [38]. Finally, Rx [29] is a library originally developed for .NET and recently ported to various platforms, including Java. Rx has received great attention since it has been successfully adopted in large-scale projects, including content distribution in the Netflix streaming media provider. Rx shares many similarities with event-based languages, including abstractions for event composition based on LINQ. The programming model of Rx is slightly different from the one offered in FRP and in DREAM. In particular, Rx provides a generic interface for event sources; the programmer can subscribe to an event source by registering a closure that gets executed when an event occurs. Even if Rx supports distributed programming, it does neither ensure consistency guarantees nor glitch freedom.

8. CONCLUSIONS
The reactive programming paradigm has been proposed to ease the development of modern reactive systems. Nevertheless, distributed reactive programming (DRP) has received little attention so far. Most significantly, existing solutions for DRP do not provide precise semantics and guarantees for the propagation of changes. This paper addressed such problem by introducing an abstract model for DRP and by formalizing some desirable consistency guarantees. Starting from this analysis, we defined three propagation semantics, we implemented them in the DREAM middleware, and we provided an extensive evaluations of their costs.

In future work, we will target both the expressiveness and the efficiency of DREAM. On the one hand, we want to investigate more complex reactive expressions (e.g., to capture time series and sequences of changes). On the other hand, we want to explore different strategies for evaluating expressions (e.g., incremental evaluation, lazy evaluation). Finally, we plan to assess the benefits of DREAM in real applications.

We hope that the content of this paper, and in particular our analysis of the consistency guarantees and our evaluation of their costs, will represent the base for future research efforts, to provide flexible and powerful abstractions and ease the development of distributed reactive systems.

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9. REFERENCES


